8 The variables $x$ and $y$ are connected by the equation

$$
y=1+2 x^{2}-x^{3} .
$$

The table below shows some values of $x$, and the corresponding values of $y$, correct to 1 decimal place where appropriate.

| $x$ | -1 | -0.5 | 0 | 0.5 | 1 | 1.5 | 2 | 2.5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 4 | 1.6 | 1 | 1.4 | 2 | 2.1 | 1 | $p$ |

(a) Calculate $p$.

Give your answer correct to 1 decimal place.

$$
\begin{equation*}
\text { Answer } \quad p= \tag{1}
\end{equation*}
$$

(b) On the graph paper opposite, using a scale of 2 cm to represent 1 unit on both axes, draw a horizontal $x$-axis for $-2 \leqslant x \leqslant 3$, and draw a vertical $y$-axis for $-3 \leqslant y \leqslant 5$.
On your axes, plot the points given in the table and join them with a smooth curve.
(c) Use your graph to find all the solutions of $1+2 x^{2}-x^{3}=2$.

$$
\begin{equation*}
\text { Answer } x= \tag{2}
\end{equation*}
$$

(d) By drawing a tangent, find the gradient of the curve at the point where $x=-0.5$.
Answer
(e) By drawing an appropriate straight line on the grid, solve the equation $1+2 x^{2}-x^{3}=x$.

$$
\text { Answer } \quad x=
$$

(f) Find the range of values of $k$ such that $1+2 x^{2}-x^{3}=k$ has 3 solutions.
Answer


