# **BINOMIAL EXPANSION**

# O/N/2006/Q1

Find the coefficient of  $x^2$  in the expansion of  $\left(x + \frac{2}{x}\right)^6$ .

[3]

O/N/2008/Q1 Find the value of the coefficient of  $x^2$  in the expansion of  $\left(\frac{x}{2} + \frac{2}{x}\right)^6$ .

[3]

M/J/2019/Q1 Find the coefficient of x in the expansion of  $\left(\frac{2}{x} - 3x\right)^5$ . [3]

O/N/2018/Q1
Find the coefficient of  $\frac{1}{x^2}$  in the expansion of  $\left(3x + \frac{2}{3x^2}\right)^7$ . [4]

O/N/2017/Q1 Find the term independent of x in the expansion of  $\left(2x - \frac{1}{4x^2}\right)^9$ .

[4]

M/J/2015/Q3
(i) Find the coefficients of  $x^2$  and  $x^3$  in the expansion of  $(2-x)^6$ . [3]

(ii) Find the coefficient of  $x^3$  in the expansion of  $(3x + 1)(2 - x)^6$ . [2]

### M/J/2017/Q1

- (i) Find the coefficient of x in the expansion of  $\left(2x \frac{1}{x}\right)^5$ . [2]
- (ii) Hence find the coefficient of x in the expansion of  $(1 + 3x^2) \left(2x \frac{1}{x}\right)^5$ . [4]

- M/J/2020/Q1
  (a) Find the coefficient of  $x^2$  in the expansion of  $\left(x \frac{2}{x}\right)^6$ . [2]
  - **(b)** Find the coefficient of  $x^2$  in the expansion of  $(2+3x^2)\left(x-\frac{2}{x}\right)^6$ . [3]

M/J/2014/Q2
Find the coefficient of  $x^2$  in the expansion of  $(1 + x^2) \left(\frac{x}{2} - \frac{4}{x}\right)^6$ . [5]

### M/J/2013/Q2

Find the coefficient of  $x^2$  in the expansion of

(i) 
$$\left(2x - \frac{1}{2x}\right)^6$$
, [2]

(ii) 
$$(1+x^2)\left(2x-\frac{1}{2x}\right)^6$$
. [3]

### M/J/2016/Q4

Find the term that is independent of x in the expansion of

(i) 
$$\left(x - \frac{2}{x}\right)^6$$
, [2]

(ii) 
$$\left(2 + \frac{3}{x^2}\right) \left(x - \frac{2}{x}\right)^6$$
. [4]

- O/N/2010/Q1 (i) Find the first 3 terms in the expansion, in ascending powers of x, of  $(1 2x^2)^8$ . [2]
  - (ii) Find the coefficient of  $x^4$  in the expansion of  $(2-x^2)(1-2x^2)^8$ . [2]

### M/J/2008/Q3

- (i) Find the first 3 terms in the expansion, in ascending powers of x, of  $(2 + x^2)^5$ . [3]
- (ii) Hence find the coefficient of  $x^4$  in the expansion of  $(1+x^2)^2(2+x^2)^5$ . [3]

## M/J/2005/Q4

- (i) Find the first 3 terms in the expansion of  $(2-x)^6$  in ascending powers of x. [3]
- (ii) Find the value of k for which there is no term in  $x^2$  in the expansion of  $(1 + kx)(2 x)^6$ . [2]

O/N/2012/Q1 In the expansion of  $\left(x^2 - \frac{a}{x}\right)^7$ , the coefficient of  $x^5$  is -280. Find the value of the constant a. [3]

O/N/2015/Q2
In the expansion of  $(x + 2k)^7$ , where k is a non-zero constant, the coefficients of  $x^4$  and  $x^5$  are equal. Find the value of k.

M/J/2018/Q1
The coefficient of  $x^2$  in the expansion of  $\left(2 + \frac{x}{2}\right)^6 + (a+x)^5$  is 330. Find the value of the constant a.

M/J/2012/Q3
The coefficient of  $x^3$  in the expansion of  $(a + x)^5 + (2 - x)^6$  is 90. Find the value of the positive constant a.

- M/J/2011/Q2
  (i) Find the terms in  $x^2$  and  $x^3$  in the expansion of  $\left(1 \frac{3}{2}x\right)^6$ . [3]
  - (ii) Given that there is no term in  $x^3$  in the expansion of  $(k+2x)(1-\frac{3}{2}x)^6$ , find the value of the constant k.

### O/N/2009/Q2

- (i) Find, in terms of the non-zero constant k, the first 4 terms in the expansion of  $(k+x)^8$  in ascending powers of x.
- (ii) Given that the coefficients of  $x^2$  and  $x^3$  in this expansion are equal, find the value of k. [2]

### O/N/2020/Q1

The coefficient of  $x^3$  in the expansion of  $(1 + kx)(1 - 2x)^5$  is 20.

Find the value of the constant k. [4]

# O/N/2016/Q4

In the expansion of  $(3-2x)\left(1+\frac{x}{2}\right)^n$ , the coefficient of x is 7. Find the value of the constant n and hence find the coefficient of  $x^2$ .

### M/J/2009/Q3

- (i) Find the first 3 terms in the expansion of  $(2 + 3x)^5$  in ascending powers of x. [3]
- (ii) Hence find the value of the constant a for which there is no term in  $x^2$  in the expansion of  $(1+ax)(2+3x)^5$ .

# O/N/2011/Q1

- (i) Find the first 3 terms in the expansion of  $(2 y)^5$  in ascending powers of y. [2]
- (ii) Use the result in part (i) to find the coefficient of  $x^2$  in the expansion of  $(2 (2x x^2))^5$ . [3]

### O/N/2014/Q3

(i) Find the first 3 terms, in ascending powers of x, in the expansion of  $(1+x)^5$ . [2]

The coefficient of  $x^2$  in the expansion of  $(1 + (px + x^2))^5$  is 95.

(ii) Use the answer to part (i) to find the value of the positive constant p. [3]

### O/N/2007/Q3

- (i) Find the first three terms in the expansion of  $(2 + u)^5$  in ascending powers of u. [3]
- (ii) Use the substitution  $u = x + x^2$  in your answer to part (i) to find the coefficient of  $x^2$  in the expansion of  $(2 + x + x^2)^5$ . [2]

# M/J/2006/Q4

The first three terms in the expansion of  $(2 + ax)^n$ , in ascending powers of x, are  $32 - 40x + bx^2$ . Find the values of the constants n, a and b.