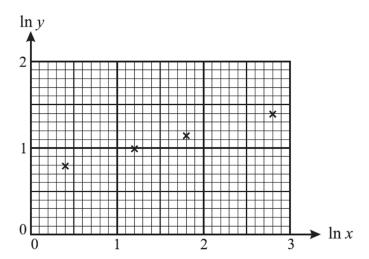
Exponential Functions

Monday, 6 June 2022

O/N/2005/Q2



Two variable quantities x and y are related by the equation $y = Ax^n$, where A and n are constants. The diagram shows the result of plotting $\ln y$ against $\ln x$ for four pairs of values of x and y. Use the diagram to estimate the values of A and n.

M/J/2006/Q1

Given that $x = 4(3^{-y})$, express y in terms of x.

[3]



Solve, correct to 3 significant figures, the equation

$$e^x + e^{2x} = e^{3x}$$
. [5]

O/N/2008/Q1

Solve the equation

$$\ln(x+2) = 2 + \ln x,$$

giving your answer correct to 3 decimal places.

[3]

M/J/2009/Q1

Solve the equation $ln(2 + e^{-x}) = 2$, giving your answer correct to 2 decimal places.

O/N/2009/Q1

Solve the equation

$$\ln(5-x) = \ln 5 - \ln x,$$

[4]

giving your answers correct to 3 significant figures.

Solve the equation

$$\ln(1+x^2) = 1 + 2\ln x,$$

giving your answer correct to 3 significant figures.

O/N/2011/Q1

Using the substitution $u = e^x$, or otherwise, solve the equation

$$e^x = 1 + 6e^{-x},$$

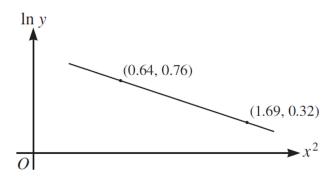
giving your answer correct to 3 significant figures.

Solve the equation

$$\ln(3x+4) = 2\ln(x+1),$$

giving your answer correct to 3 significant figures.

M/J/2013/Q3



The variables x and y satisfy the equation $y = Ae^{-kx^2}$, where A and k are constants. The graph of $\ln y$ against x^2 is a straight line passing through the points (0.64, 0.76) and (1.69, 0.32), as shown in the diagram. Find the values of A and k correct to 2 decimal places. [5]

$$2\ln(5 - e^{-2x}) = 1,$$

giving your answer correct to 3 significant figures.

O/N/2014/Q1

Use logarithms to solve the equation $e^x = 3^{x-2}$, giving your answer correct to 3 decimal places. [3]



Solve the equation $ln(x^2 + 1) = 1 + 2 ln x$, giving your answer correct to 3 significant figures. [3]

O/N/2018/Q4

Showing all necessary working, solve the equation

$$\frac{e^x + e^{-x}}{e^x + 1} = 4,$$

[5]

giving your answer correct to 3 decimal places.



Solve the equation $5 \ln(4 - 3^x) = 6$. Show all necessary working and give the answer correct to 3 decimal places. [3]